

Name Answer key
 Calc I H -1.2-1.3 Review

Date _____
 Period _____

1. Find the value of the limit $\lim_{x \rightarrow -1} \frac{x^2 + 2x + 1}{x^2 - x - 2}$. = $\lim_{x \rightarrow -1} \frac{(x+1)^2}{(x-2)(x+1)} = \lim_{x \rightarrow -1} \frac{x+1}{x-2} = 0$
- A) 1 B) 2 C) -2 **D) 0**
 E) -1 F) $\frac{1}{2}$ G) $-\frac{1}{2}$ H) does not exist

2. Find the value of the limit $\lim_{x \rightarrow 1} \frac{x-1}{x^4-1}$. = $\lim_{x \rightarrow 1} \frac{\cancel{x-1}}{(x+1)\cancel{(x-1)}(x^2+1)} = \lim_{x \rightarrow 1} \frac{1}{(x+1)(x^2+1)} = \frac{1}{2 \cdot 2} = \frac{1}{4}$
- A) 0 B) 2 C) 4 D) 8
E) $\frac{1}{4}$ F) $\frac{1}{8}$ G) $\frac{1}{32}$ H) $\frac{1}{64}$

3. Suppose that $\lim_{x \rightarrow c} f(x) = -9$ and $\lim_{x \rightarrow c} g(x) = 14$. Find $\lim_{x \rightarrow c} [f(x) - g(x)]$. = $\lim_{x \rightarrow c} f(x) - \lim_{x \rightarrow c} g(x) = -9 - 14 = -23$
- A) -9 B) 14 **C) -23** D) 23
 E) -5 F) 5 G) -14 H) does not exist

4. Find the value of the limit $\lim_{x \rightarrow 4} \frac{x-4}{\sqrt{x}-2}$. = $\lim_{x \rightarrow 4} \frac{\cancel{(x-4)}(\sqrt{x}+2)}{\sqrt{x}-2} = \lim_{x \rightarrow 4} (\sqrt{x}+2) = \sqrt{4}+2 = 4$
- A) 0 B) 2 **C) 4** D) 8
 E) $\frac{1}{4}$ F) $\frac{1}{8}$ G) $\frac{1}{32}$ H) $\frac{1}{64}$

5. Find the value of the limit $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x^2 - 5x + 6}$. = $\lim_{x \rightarrow 2} \frac{(x+3)\cancel{(x-2)}}{(x-3)\cancel{(x-2)}} = \lim_{x \rightarrow 2} \frac{x+3}{x-3} = \frac{2+3}{2-3} = -5$
- A) -5** B) -3 C) -1 D) 0
 E) 1 F) 3 G) 5 H) 6

6. Write the 2 special trig limits from Section 1.3:

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1 \qquad \lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$

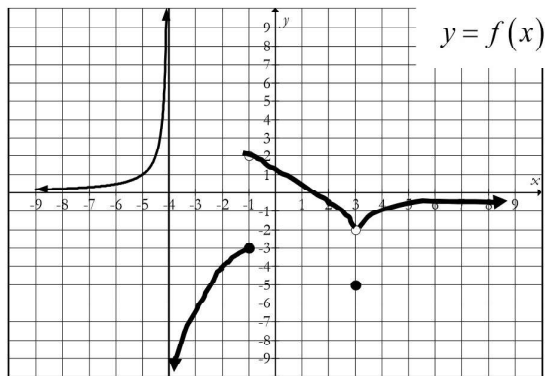
7. Find the following limits algebraically. Show your work.

<p>a. $\lim_{x \rightarrow 0} \frac{10 - 10 \cos(3x)}{4x} = \lim_{x \rightarrow 0} \frac{10}{4} \cdot \frac{(1 - \cos(3x))}{x}$</p> <p>$= \lim_{x \rightarrow 0} \left[\frac{30}{4} \cdot \frac{1 - \cos(3x)}{3x} \right]$</p> <p>$= \frac{30}{4} \cdot 0 = 0$</p>	<p>b. $\lim_{x \rightarrow 0} \frac{(3x)^2 + 1}{1 - \sin(x)} = \frac{0^2 + 1}{1 - \sin 0} = \frac{1}{1} = 1$</p>
<p>c. $\lim_{x \rightarrow 0} \frac{\tan(7x)}{x} = \lim_{x \rightarrow 0} \frac{\sin(7x)}{\cos(7x)} \cdot \frac{1}{x}$</p> <p>$= \lim_{x \rightarrow 0} \frac{7 \sin(7x)}{7x} \cdot \frac{1}{\cos(7x)}$</p> <p>$= 7 \cdot 1 \cdot \frac{1}{\cos(0)} = 7$</p>	<p>d. $\lim_{x \rightarrow 0} \frac{x - 2 \sin(3x)}{x} = \lim_{x \rightarrow 0} \left[\frac{x}{x} - \frac{2 \sin(3x)}{x} \right]$</p> <p>$= \lim_{x \rightarrow 0} \left[1 - \frac{2 \cdot 3 \sin(3x)}{3x} \right]$</p> <p>$= \lim_{x \rightarrow 0} \left[1 - 6 \lim_{x \rightarrow 0} \frac{\sin(3x)}{3x} \right] = 1 - 6 \cdot 1 = -5$</p>
<p>e. $\lim_{x \rightarrow 0} \frac{\sin 6x}{x} \cdot \frac{6}{6} = \lim_{x \rightarrow 0} \left(6 \cdot \frac{\sin 6x}{6x} \right)$</p> <p>$= 6 \cdot 1 = 6$</p>	<p>f. $\lim_{x \rightarrow 0} \frac{5(1 - \cos x)}{x} = 5 \lim_{x \rightarrow 0} \frac{1 - \cos x}{x}$</p> <p>$= 5 \cdot 0 = 0$</p>
<p>g. $\lim_{x \rightarrow 4} \frac{x - 4}{x^2 - x - 12} = \lim_{x \rightarrow 4} \frac{x - 4}{(x - 4)(x + 3)}$</p> <p>$= \lim_{x \rightarrow 4} \frac{1}{x + 3} = \frac{1}{7}$</p>	<p>h. $\lim_{x \rightarrow 0} \left(\frac{1}{x+5} - \frac{1}{5} \right) \cdot \frac{5(x+5)}{5(x+5)}$</p> <p>$= \lim_{x \rightarrow 0} \frac{5 - (x+5)}{5x(x+5)} = \lim_{x \rightarrow 0} \frac{-x}{5x(x+5)}$</p> <p>$= \lim_{x \rightarrow 0} \frac{-1}{5(x+5)} = \frac{-1}{25}$</p>
<p>i. $\lim_{x \rightarrow 14} \frac{\sqrt{x-5} - 3}{x-14} \cdot \frac{\sqrt{x-5} + 3}{\sqrt{x-5} + 3}$</p> <p>$\lim_{x \rightarrow 14} \frac{x-5-9}{(x-14)(\sqrt{x-5} + 3)} = \lim_{x \rightarrow 14} \frac{x-14}{(x-14)(\sqrt{x-5} + 3)}$</p> <p>$= \lim_{x \rightarrow 14} \frac{1}{\sqrt{x-5} + 3} = \frac{1}{\sqrt{9} + 3} = \frac{1}{6}$</p>	<p>j. $\lim_{t \rightarrow \pi} \frac{\sin t}{\tan t} = \lim_{t \rightarrow \pi} \frac{\sin t}{\frac{\sin t}{\cos t}}$</p> <p>$= \lim_{t \rightarrow \pi} \sin t \cdot \frac{\cos t}{\sin t} = \lim_{t \rightarrow \pi} \cos t$</p> <p>$= \cos \pi = -1$</p>

8. Given: $f(x) = \begin{cases} -x^2 + 2, & x < -3 \\ 2x - 1, & -3 \leq x < 1 \\ |x - 4|, & x \geq 1 \end{cases}$, evaluate each of the following:

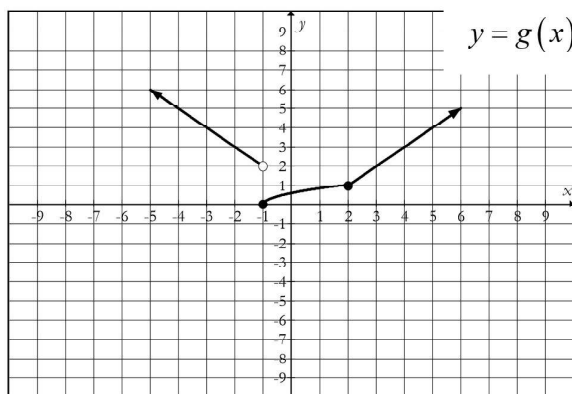
a. $\lim_{x \rightarrow -3^-} f(x) = -7$ $-(-3)^2 + 2$	b. $\lim_{x \rightarrow -3^+} f(x) = -7$ $2(-3) - 1$	c. $\lim_{x \rightarrow -3} f(x) = -7$	d. $f(-3) = -7$ $2(-3) - 1$
e. $f(1) = 3$ $ 1 - 4 $	f. $\lim_{x \rightarrow 1^-} f(x) = 1$ $2(1) - 1$	g. $\lim_{x \rightarrow 1^+} f(x) = 3$ $ 1 - 4 $	h. $\lim_{x \rightarrow 1} f(x) = \text{DNE}$

9. Use the graph below to find the following limits.



- (a) $\lim_{x \rightarrow -1} f(x) = -3$
- (b) $\lim_{x \rightarrow -1^+} f(x) = 2$
- (c) $\lim_{x \rightarrow -1} f(x) = \text{DNE}$
- (d) $f(3) = -5$
- (e) $\lim_{x \rightarrow 3} f(x) = -2$
- (f) $\lim_{x \rightarrow -4} f(x) = \text{DNE}$

10. Use the graph below to find the following limits.



- (a) $\lim_{x \rightarrow -3} g(x) = 4$
- (b) $g(-1) = 0$
- (c) $\lim_{x \rightarrow -1} g(x) = \text{DNE}$
- (d) $\lim_{x \rightarrow 2} g(x) = 1$
- (e) $\lim_{x \rightarrow 4} g(x) = 3$

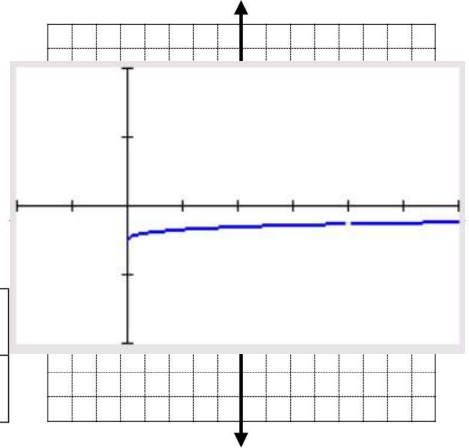
11. Use a graphing utility to graph the function and to sketch and estimate the limit. (Note: Use zoom feature to see graph better or change window on calculator as necessary.) Use a table to reinforce your conclusion. Then find the limit by analytic methods.

a. $\lim_{x \rightarrow 4} \frac{2 - \sqrt{x}}{x - 4}$

Estimate: $x = -.25$

Tabular Approx:

x	3.9	3.99	3.999	4	4.001	4.01	4.1
y	-.252	-.2502	-.25	—	-.25	-.2498	-.249



Analytic: (Show all work and watch the notation!)

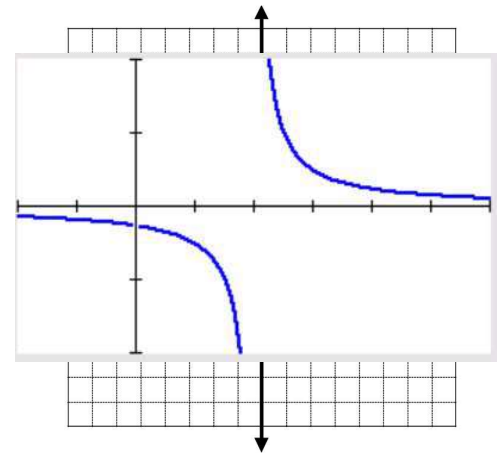
$$\frac{0}{0} \quad \lim_{x \rightarrow 4} \frac{(2 - \sqrt{x})(2 + \sqrt{x})}{(x - 4)(2 + \sqrt{x})} = \lim_{x \rightarrow 4} \frac{4 - x}{(x - 4)(2 + \sqrt{x})} = \lim_{x \rightarrow 4} \left(\frac{-1}{2 + \sqrt{x}} \right) = \frac{-1}{2 + \sqrt{4}} = \frac{-1}{4}$$

b. $\lim_{x \rightarrow 0} \frac{\frac{1}{2} + \frac{1}{x-2}}{x}$

Estimate: $x = -.25$

Tabular Approx: $x = -.25$

x	-.1	-.01	-.001	0	.001	.01	.1
y	-.2381	-.2488	-.2499	—	-.2501	-.2513	-.262



Analytic: (Show all work and watch the notation!)

$$\lim_{x \rightarrow 0} \frac{\left(\frac{1}{2} + \frac{1}{x-2}\right) 2(x-2)}{x \cdot 2(x-2)} = \lim_{x \rightarrow 0} \frac{x-2+2}{2x(x-2)} = \lim_{x \rightarrow 0} \frac{x}{2x(x-2)} = \lim_{x \rightarrow 0} \frac{1}{2(x-2)} = \frac{-1}{4}$$