

Name _____

Date _____

Calc I H - Chapter 5 Derivatives Review

Period _____

Do you remember the rules for finding the derivative of exponential and natural log functions?

$$\frac{d}{dx}[e^x] = e^x$$

$$\frac{d}{dx}[e^u] = e^u u'$$

$$\frac{d}{dx}[\ln(x)] = \frac{1}{x}$$

$$\frac{d}{dx}[\ln(u)] = \frac{1}{u} \cdot u' = \frac{u'}{u}$$

Find the derivative of each function.

$$1) f(x) = e^{5x^2+1}$$

$$f'(x) = e^{5x^2+1} \cdot 10x$$

$$f'(x) = 10x e^{5x^2+1}$$

$$2) y = \ln(3x^3 + 4x)$$

$$y' = \frac{1}{3x^3+4x} (9x^2+4) = \frac{9x^2+4}{3x^3+4x}$$

$$3) g(x) = e^{(3x^2+1)^2}$$

$$g'(x) = 2(3x^2+1)(6x)e^{(3x^2+1)^2}$$

$$g'(x) = 12x(3x^2+1)e^{(3x^2+1)^2}$$

$$4) p(x) = \ln\left(\frac{5x^2}{3x+1}\right)$$

$$p(x) = \ln 5x^2 - \ln(3x+1)$$

$$p'(x) = \frac{1}{5x^2}(10x) - \frac{1}{3x+1}(3)$$

$$p'(x) = \frac{2}{x} - \frac{3}{3x+1}$$

5) What is the equation of the tangent line to $y = \ln e^{5x^2}$ at the point where $x = 3$?

Slope

$$y' = \frac{1}{e^{5x^2}}(10x)e^{5x^2}$$

$$y' = 10x$$

$$y'(3) = 10(3)$$

$$y'(3) = 30$$

Point

$$y(3) = \ln e^{5(3)^2}$$

$$= \ln e^{45}$$

$$y(3) = 45$$

$$(3, 45)$$

Tangent Line

$$y - 45 = 30(x - 3)$$

Practice in your groups:

$$6) \frac{d}{dx} \left[e^{\frac{x^5}{2}} \right] = \frac{5}{2} x^4 e^{\frac{x^5}{2}}$$

$$= \frac{5x^4 e^{\frac{x^5}{2}}}{2}$$

$$7) \frac{d}{dx} \left[\ln(4x^2(3x+2)^2) \right] =$$

$$\frac{d}{dx} \left[\ln 4x^2 + \ln(3x+2)^2 \right]$$

$$\frac{d}{dx} \left[\ln 4 + 2 \ln x + 2 \ln(3x+2) \right] = 0 + 2 \left(\frac{1}{x} \right) + 2 \left(\frac{3}{3x+2} \right)$$

$$= \frac{2}{x} + \frac{6}{3x+2}$$

$$8) \frac{d}{dx} \left[5xe^{3x^5} \right] = 5e^{3x^5} + 5x(15x^4)e^{3x^5}$$

$$= 5e^{3x^5} + 75x^5 e^{3x^5}$$

or

$$5e^{3x^5} (1 + 15x^5)$$

$$9) \frac{d}{dx} \left[\ln(e^{x^4}) \right] = \frac{1}{e^{x^4}} (4x^3 e^{x^4})$$

$$= 4x^3$$

or

$$\frac{d}{dx} (x^4) = 4x^3$$

10) Find the slope of the tangent line to the function at the given point:

a. $f(x) = e^{3x^2}$ at $(2, e^{12})$

$$f'(x) = 6xe^{3x^2}$$

Slope

$$f'(2) = 6(2)e^{3(2)^2}$$

$$= 12e^{12}$$

$$y - e^{12} = 12e^{12}(x - 2)$$

b. $g(x) = \ln\left(\frac{3x}{2}\right)$ at $(4, \ln(6))$

$$g'(x) = \frac{1}{\frac{3x}{2}} \cdot \frac{3}{2} = \frac{1}{x}$$

Slope

$$g'(4) = \frac{1}{4}$$

$$y - \ln(6) = \frac{1}{4}(x - 4)$$

11) Write down the equation of the tangent line to the given function at the given x-coordinate.

a. $h(x) = 4xe^{x^3}$ at $x = -2$

$$h'(x) = 4e^{x^3} + 4x(3x^2)e^{x^3}$$

$$= 4e^{x^3} + 12x^3 e^{x^3}$$

Slope

$$h'(-2) = 4e^{(-2)^3} + 12(-2)^3 e^{(-2)^3}$$

$$= 4e^{-8} - 96e^{-8}$$

$$= -92e^{-8}$$

Point

$$h(-2) = 4(-2)e^{(-2)^3}$$

$$= -8e^{-8}$$

$$(-2, -8e^{-8})$$

$$y + 8e^{-8} = -92e^{-8}(x + 2)$$

b. $p(x) = \ln(5x^2 + 1)$ at $x = 2$

$$p'(x) = \frac{1}{5x^2 + 1} (10x) = \frac{10x}{5x^2 + 1}$$

Slope

$$p'(2) = \frac{10(2)}{5(2)^2 + 1}$$

$$= \frac{20}{21}$$

Point

$$p(2) = \ln(5(2)^2 + 1)$$

$$= \ln(21)$$

$$(2, 21)$$

$$y - 21 = \frac{20}{21}(x - 2)$$